

Antidifferentiation (shmoo) is also known as indefinite integration and is denoted with the symbol $\int dx$

Ex $\int x^2 dx = \frac{1}{3}x^3 + C$

"the antiderivative of f with respect to x "
or "the integral of f with respect to x "

$$\int f(x) dx = F(x) + C$$

variable of integration

↑
integrand

↑
constant of integration

INTEGRATION RULES

POWER RULE

$$\int x^n dx = \frac{1}{n+1} x^{n+1} + C ; n \neq -1$$

CONSTANT RULE

$$\int k dx = kx + C$$

CONSTANT MULTIPLE RULE

$$\int k f(x) dx = k \int f(x) dx$$

SUM OR DIFFERENCE RULE

$$\int (f(x) \pm g(x)) dx = \int f(x) dx \pm \int g(x) dx$$

Ex] a) $\int x^4 dx = \frac{1}{5}x^5 + C$

b) $\int 4 dt = 4t + C$

c) $\int 3x^5 dx = 3 \int x^5 dx = 3 \left(\frac{1}{6} x^6 \right) + C$
 $= \frac{1}{2} x^6 + C$

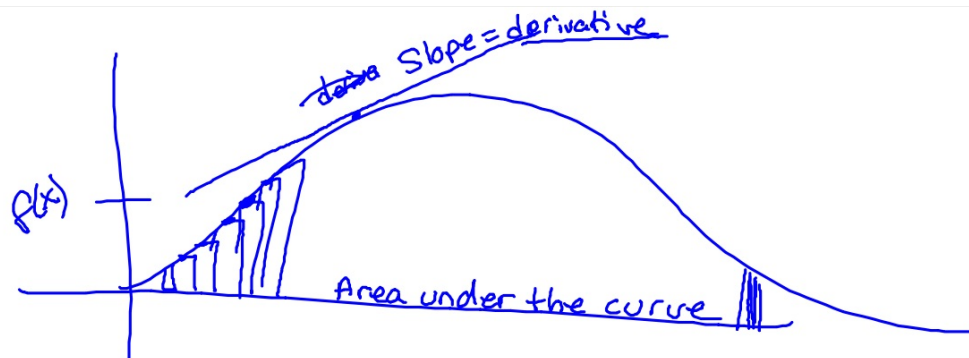
d) $\int (3u^4 + 6u^2 + 2) du$

$$= \int 3u^4 du + \int 6u^2 du + \int 2 du$$

$$= 3 \int u^4 du + 6 \int u^2 du + \int 2 du$$

$$= 3 \left(\frac{1}{5} u^5 \right) + 6 \left(\frac{1}{3} u^3 \right) + 2u + C$$

$$= \frac{3}{5} u^5 + 2u^3 + 2u + C$$



$$\sum_{i=1}^n f(x_i) \Delta x$$

$$\int \underbrace{-(x-8)^2 + 5}_{\text{height}} \underbrace{dx}_{\text{width}}$$

HW 9B p 294
1-11 odd 296
1-11 ac. P. 3, 5

$$\begin{aligned} \int (x + \sqrt[3]{x}) dx &= \int x dx + \int x^{\frac{1}{3}} dx \\ &= \frac{1}{2}x^2 + \frac{3}{4}x^{\frac{4}{3}} + C \end{aligned}$$

Finding C

$$s(t) = t^2 + t + C$$

$$v(t) = 2t + 1$$

What was the position
at time $t = 6$ sec?
We're given that the
position is 1 m.

$$1 = (6)^2 + 6 + C$$

$$1 = 36 + 6 + C$$

$$1 = 42 + C$$

$$-41 = C$$

$$s(t) = t^2 + t - 41$$