

equation of a line  $y = mx + b$

$$y - y_1 = m(x - x_1)$$

$$y - y_1 = \frac{dy}{dx} (x - x_1)$$

↑  
derivative  
of the function

$(x_1, y_1)$  is  
a point on  
the curve

Ex) Write the equation of the line tangent to  $f(x) = x^3 - 3x^2 - 13x + 15$  that is parallel to the tangent at  $(4, -21)$

$$f(x) = x^3 - 3x^2 - 13x + 15$$

$$f'(x) = 3x^2 - 6x - 13$$

$$f'(4) = 3(4)^2 - 6(4) - 13$$

$$= 3(16) - 24 - 13$$

$$f'(4) = 11$$



Set derivative = to 11 (slope) and find the other  $x$

$$3x^2 - 6x - 13 = 11$$

$$\text{solve} \rightarrow 3x^2 - 6x - 24 = 0$$

$$3x^2 - 6x - 24 = 0$$
$$3(x^2 - 2x - 8) = 0$$
$$3(x - 4)(x + 2) = 0$$

$$x = 4 \quad x = -2$$

HW 7G p. 207  
# 2, 3, 4, 5

This function has a tangent line  
with slope (gradient) of 11 at  
 $x = 4$  and  $x = -2$

plug  $x = -2$  into  $f(x)$  to find  $y$  of  
point

$$f(-2) = (-2)^3 - 3(-2)^2 - 13(-2) + 15$$
$$= 21$$

• • point  $(-2, 21)$

$$y - 21 = 11(x + 2)$$