

$$3a) X \sim B(15, 0.25)$$

$$b) \text{ mean} = X \times 0.25 = 3.75$$

$$c) P(X \geq 10) =$$

$$1 - \binom{15}{9} (.25)^9 (.75)^6 =$$

$$\binom{15}{10}$$

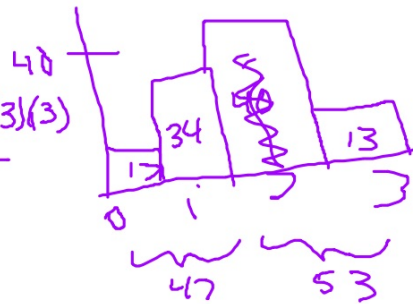
$$7.949 \times 10^{-4}$$

$$0.000795$$

4a) $P(g)$

# of girls	0	1	2	3
Frequency	13	34	40	13

$$\frac{(13 \times 0) + (34 \times 1) + (2 \times 40) + (3 \times 13)}{100}$$



15.3 The Normal Distribution

- no single normal curve
- a family of curves defined by their mean μ and std dev σ ,

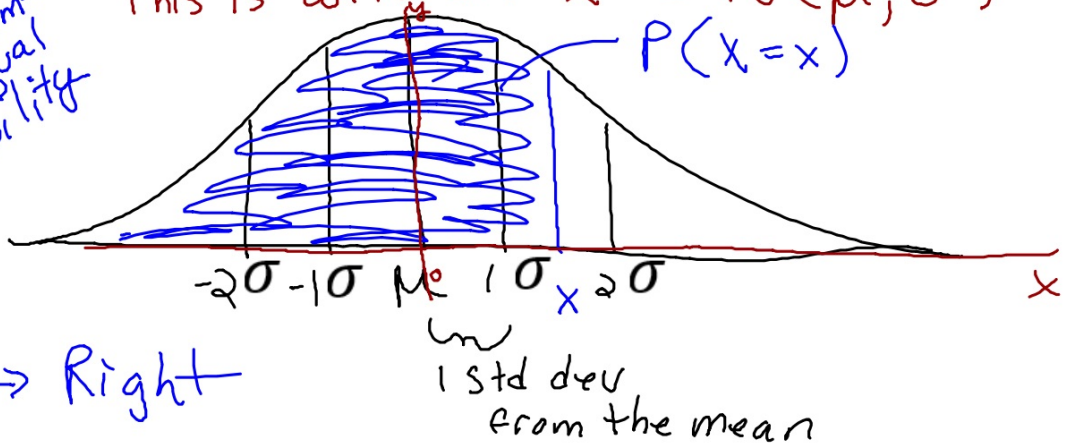
Recall: μ = mean central point of dist
 σ = std dev - describes spread
 σ^2 = Variance

how far you are from the mean

If a random variable X , has normal distribution with mean μ and std dev σ
This is written $X \sim N(\mu, \sigma^2)$

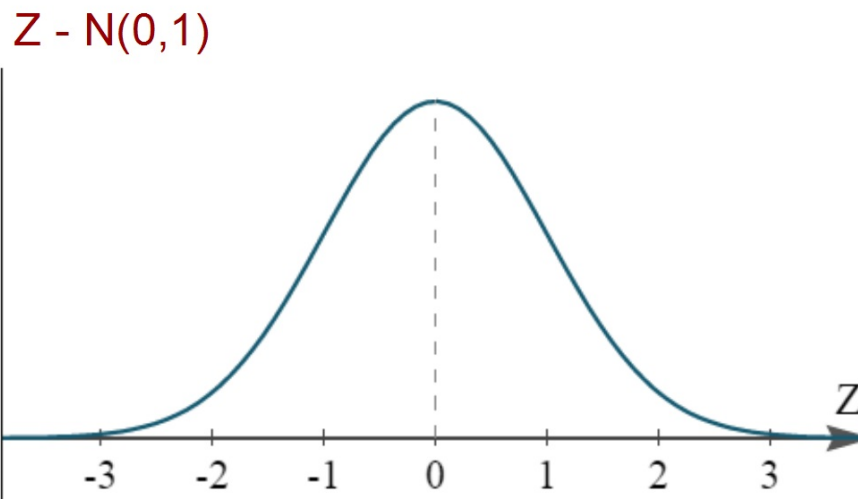
The Area under the curve (cumulative) is equal to the probability $P(X \leq x)$

Left \rightarrow Right



The Standard Normal Distribution:

- is the Normal Distribution where $\mu=0$ and $\sigma=1$. The random variable is Z and uses 'z-scores' or 'z-values' to describe the number of standard deviations any value is away from the mean.



2nd
VARS

USING CALCULATOR TO FIND Z-VALUE:

normalcdf(lower limit, upper limit, μ , σ)



Ex) $Z \sim N(0, 1)$ FIND

a) $P(-2 < Z < 1) = 0.819$



b) $P(Z < 1) = 0.841$



c) $P(Z > -1.5) = 0.933$



d) $P(|Z| > 0.8) = 0.424$

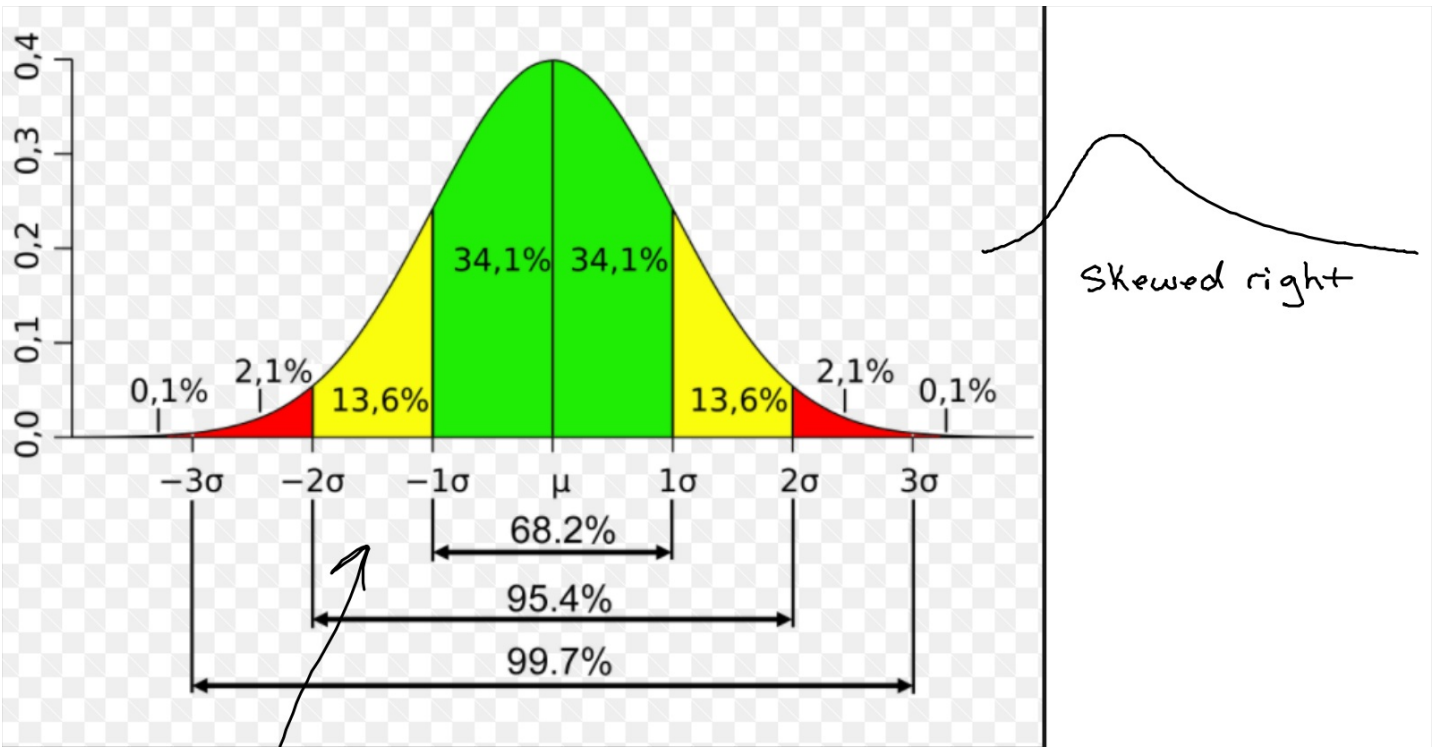
$1 - \text{normalcdf}(-0.8, 0.8, 0, 1)$



cdf - cumulative prob for an area

pdf - probab. for 1 #

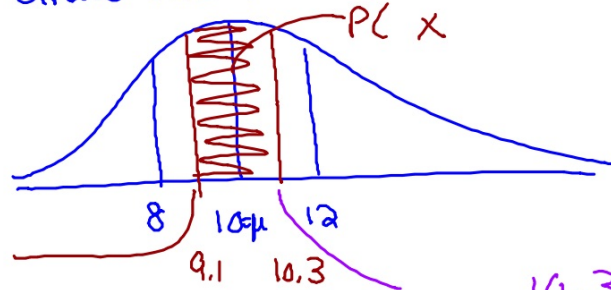
HW 15H
1, 6



THIS OCCURS IN A PERFECT WORLD
 BUT, WE CAN TAKE ANY NORMAL DIST $X \sim N(\mu, \sigma)$
 AND TRANSFORM IT TO STD NORMAL
 BY ACCOUNTING FOR ANY SHIFTS OR CHANGES IN SPREAD

IF $X \sim N(\mu, \sigma^2)$ THEN THE TRANSFORMED
RANDOM VARIABLE $Z = \frac{X - \mu}{\sigma}$ HAS A TRANSFORMED
NORMAL DIST

Ex] $X \sim N(10, 2)$, FIND $P(9.1 < x < 10.3)$
1st draw the curve + i.d. the area



$$z = \frac{9.1 - 10}{2} = -0.45$$

$$z = \frac{10.3 - 10}{2} = 0.15$$

$$P(9.1 < x < 10.3) = P(-0.45 < Z < 0.15)$$

$$= \text{normalcdf}(-.45, 0.15, 0, 1)$$

$$= 0.233$$

P. 543

HW 15I
1-3

z?