

$$\begin{aligned}
 4m \quad 2e &= 3\ln 2 - 2 \\
 &= \ln 2^3 - \ln e^2 \\
 &= \ln 8 - \ln e^2 \\
 &= \ln \left(\frac{8}{e^2} \right)
 \end{aligned}$$

$$\begin{aligned}
 3e \quad \frac{1}{2} \log 36 - \log 15 + 2 \log 5 \\
 &= \log 6 - (\log 15 + \log 25) \\
 &= \log \left(\frac{6}{15} \right) + \log 25 \\
 &= \log \left(\frac{6^2}{15^2} \cdot 25 \right) = \log \left(\frac{50}{3} \right)
 \end{aligned}$$

$$\log_{10} 10 = y = \log(10)$$

$$10^y = 10^1$$

$$y = 1$$

$$4N \quad 2. \log\left(\frac{P^2}{QR^2}\right)^3 = 3\log\left(\frac{P^2}{QR^2}\right)$$

$$\begin{aligned} x &= \log P \\ y &= \log Q \\ z &= \log R \end{aligned}$$

$$= 3[\log(P^2) - \log(QR^2)]$$

$$= 3[2\log P - (\log Q + 2\log R)]$$

$$= 3[2x - (y + 2z)]$$

$$= 6x - 3(y + 2z)$$

$$= 6x - 3y - 6z$$

4. $y = \log_3 \frac{27^a}{81}$ in form $y = pa + q$
 $p, q \in \mathbb{Z}$

$$\log_3(27) = p = \log_3(27^a) - \log_3(81)$$

$$p = 27$$

$$3^p = 27$$

$$3^p = 3^3$$

$$= a \log_3(27) - \log_3(81)$$

$$3^x = 27$$

$$= 3a - 4$$

$$\begin{aligned} \log_3(81) &= q \\ 3^q &= 81 \\ q &= 4 \end{aligned}$$

6. $e^{\ln 2^x} = 2^x$ show it's true

$$\frac{e^{\ln 2^x}}{2^x}$$

$$\sin^{-1}(\sin(x)) = \sin^{-1}\left(\frac{1}{2}\right)$$

$$x = 60^\circ$$

$$e^{\ln(x)} = e^4$$

$$\rightarrow x =$$

$$e^4$$

Questions:

Notes:

CHANGE OF BASE

Recall: if we have $\log(x) = \#$
can apply $10^{\log(x)} = 10^{\#}$
 $x = 10^{\#}$

$$\bullet \log_b a = \frac{\log_c a}{\log_c b}$$

FOR USE IN CALCULATOR

EX EVALUATE $\log_4 9$ to 3sf.

$$\log_4 9 = \frac{\log_{10} 9}{\log_{10} 4} \approx 1.58$$

EX $a = \log_x 3$ and $b = \log_x 6$

find $\log_3 6$ in terms of a and b

$$\log_3 6 = \frac{\log 6}{\log 3} = \frac{b}{a}$$

HW 40 p. 126 1) 2, 3, 5b