

Questions:

Notes:

$$\#5 \quad n = 4000 e^{.08t}$$

good to know!

4T #5

$$32 = a \cdot 2^b \qquad 108 = a \cdot 3^b$$

$$\ln 32 = \ln(a \cdot 2^b)$$

$$\ln 32 = \ln a + b \ln 2$$

$$\ln 32 = \ln a + b \ln 2 \qquad \ln 108 = \ln a + b \ln 3$$

$$\ln a = \ln 32 - b \ln 2 \qquad \ln a = \ln 108 - b \ln 3$$

$$\ln 32 - b \ln 2 = \ln a$$

$$\ln 32 - b \ln 2 = \ln 108 - b \ln 3$$

$$-b \ln 2 = \ln 108 - b \ln 3 - \ln 32$$

$$b \ln 3 - b \ln 2 = \ln 108 - \ln 32$$

$$b \ln\left(\frac{3}{2}\right) = \ln\left(\frac{108}{32}\right)$$

$$b(\ln 3 - \ln 2)$$

$$b = \frac{\ln 108 - \ln 32}{\ln\left(\frac{3}{2}\right)}$$

$$b = 3$$

$$\ln a = \ln 32 - 3 \ln 2$$

$$\ln a = \ln\left(\frac{32}{2^3}\right)$$

$$a = \frac{32}{8} = 4$$



Questions:

Notes: Review #8

a.  $f(x) = 3e^{2x}$  Find  $f^{-1}(x)$

$$y = 3e^{2x}$$
$$\frac{x}{3} = \frac{3e^{2y}}{3}$$

$$\frac{x}{3} = e^{2y}$$

$$\ln\left(\frac{x}{3}\right) = \ln e^{2y}$$

$$\ln\left(\frac{x}{3}\right) = 2y$$

$$\frac{\ln\left(\frac{x}{3}\right)}{2} = y$$

- ① replace  $f(x)$  with  $y$
- ② switch  $x$  and  $y$
- ③ divide both by 3

- ④ take  $\ln$  of both sides  
-  $\ln$  and  $e$  cancel each other

- ⑤ divide by 2

- ⑥ replace  $y$  with  $f^{-1}$

8c.  $f(x) = \log_2(4x)$

$$y = \log_2(4x)$$

$$x = \log_2(4y)$$

①  $f(x) = y$

②  $x \leftrightarrow y$

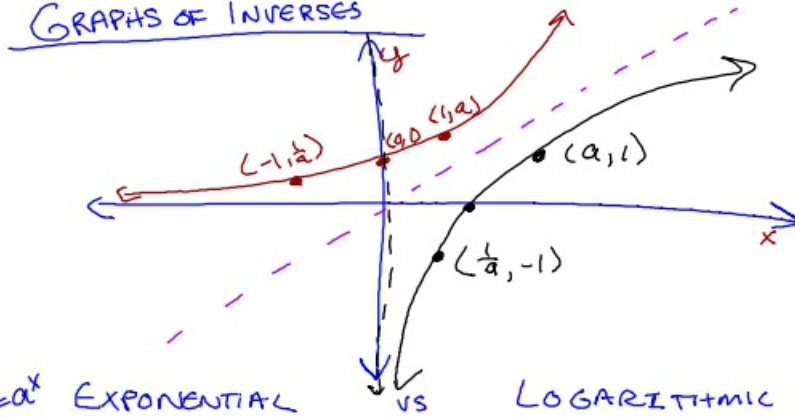
- ③ Switch to equivalent exponent

$$\frac{2^x}{4} = \frac{4y}{4}$$

$$y = \frac{2^x}{4} = \frac{2^x}{2^2} = 2^{(x-2)}$$

$$\frac{2^5}{2^2} = 2^3 = 8$$

# GRAPHS OF INVERSES



$y = a^x$  EXPONENTIAL

INCREASING  
HORIZONTAL asym.  $y = 0$

DOMAIN:  $\mathbb{R}$

RANGE:  $\mathbb{R}^+$   $y > 0$

y-int:  $(0, 1)$

LOGARITHMIC  $y = \log_a(x)$

INCREASING  
VERTICAL asym.  $x = 0$

RANGE:  $\mathbb{R}$

DOMAIN:  $\mathbb{R}^+$

x-int:  $(1, 0)$

vs  
REFLECT OVER  $y = x$   
 $(x, y) \rightarrow (y, x)$

