

Solve
by CTS

2D #4

$$\frac{4x^2}{4} + \frac{6x}{4} - \frac{5}{4} = 0$$

$$\cancel{\frac{4}{4}} (x^2 + \frac{3}{2}x - \frac{5}{4}) = 0$$

$$x^2 + \frac{3}{2}x - \frac{5}{4} = 0$$

$$x^2 + \frac{3}{2}x + \frac{9}{16} = \frac{5}{4} + \frac{9}{16}$$

$$\left(\frac{3}{2}\right)^2$$

$$\left(\frac{3}{2}\right)^2 = \frac{9}{4}$$

$$\sqrt{\left(x + \frac{3}{2}\right)^2} = \sqrt{\frac{29}{4}}$$

$$x + \frac{3}{2} = \frac{\pm\sqrt{29}}{2}$$

$$x = -\frac{3}{2} \pm \frac{\sqrt{29}}{2}$$

2-2 The Quadratic Formula

$$ax^2 + bx + c = 0 \quad ; \text{ say } a=1$$

complete the square:

$$x^2 + \frac{b}{a}x + \frac{c}{a} = 0$$

$$\frac{1}{2} \left(\frac{b}{a} \right) = \frac{b}{2a}$$
$$\left(\frac{b}{2a} \right)^2 = \frac{b^2}{4a^2}$$

$$x^2 + \frac{b}{a}x + \left(\frac{b}{2a} \right)^2 = -\frac{c}{a} + \left(\frac{b}{2a} \right)^2$$

$$\left(x + \frac{b}{2a} \right)^2 = \frac{4a}{4a} \left(-\frac{c}{a} + \frac{b^2}{4a^2} \right)$$

$$\left(x + \frac{b}{2a} \right)^2 = \frac{-4ac + b^2}{4a^2}$$

$$x + \frac{b}{2a} = \frac{\pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = -\frac{b}{2a} \pm \frac{\sqrt{b^2 - 4ac}}{2a}$$

$$= \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

The Quadratic Equation!

Ex] Solve $2x^2 - 3x = 7$ using the Quadratic Formula

$$\begin{aligned}x &= \frac{3 \pm \sqrt{(-3)^2 - 4(2)(-7)}}{2(2)} \\&= \frac{3 \pm \sqrt{9 + 56}}{4} \\&= \frac{3 \pm \sqrt{65}}{4}\end{aligned}$$

$$\begin{aligned}a &= 2 \\b &= -3 \\c &= -7\end{aligned}$$

Consecutive numbers

1st $x = 17$
next $x+1 = 18$

$x = -18$
 $x+1 = -17$

Ex) The sum of the squares ~~of~~ ^{of} two consecutive numbers is 613.
Find the two numbers.

$$x^2 + (x+1)^2 = 613$$

$$x^2 + x^2 + 2x + 1 = 613$$

$$2x^2 + 2x - 612 = 0$$

$$x^2 + x - 306 = 0$$

$$x = \frac{-1 \pm \sqrt{(1)^2 - 4(1)(-306)}}{2(1)}$$

$$= \frac{-1 \pm \sqrt{1225}}{2} = \frac{-1 \pm 35}{2}$$

$x = \frac{-36}{2}$ or $x = \frac{34}{2}$

$x = -18$ or $x = 17$

~~$x = 17$ or $x = 18$~~

divide all by 2

HW 2E 2-8 even
9,10

2F 1,3,4

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