

3.4 Conditional Probability

Def: Conditional Probability occurs when the outcome of event A is dependent on the outcome of B.

Ex: A bag has 3 red marbles and 2 blue. Take one out and do not replace it. total # marbles = 5

What is the probability of choosing blue on the next choice?

$$\text{1st marble } P(\text{Blue}) = \frac{2}{5}$$

2nd marble:

$$\text{if the 1st was red, } P(B) = \frac{2}{4} = \frac{1}{2}$$

$$\text{if the 1st was blue, } P(B) = \frac{1}{4}$$

In general, for two events A and B, the Probability of A occurring given that B has occurred can be found using:

$$P(A|B) = \frac{P(A \cap B)}{P(B)}$$

↑
"The Probability of A, given B"

$$\text{or } P(A \cap B) = P(A|B) \cdot P(B)$$

* if A and B are independent events,

$$\text{then } P(A|B) = \frac{P(A \cap B)}{P(B)} = \frac{P(A) \cdot P(B)}{P(B)} = P(A)$$

Ex: 53 people
 36 drink tea
 18 drink coffee
 10 drink neither

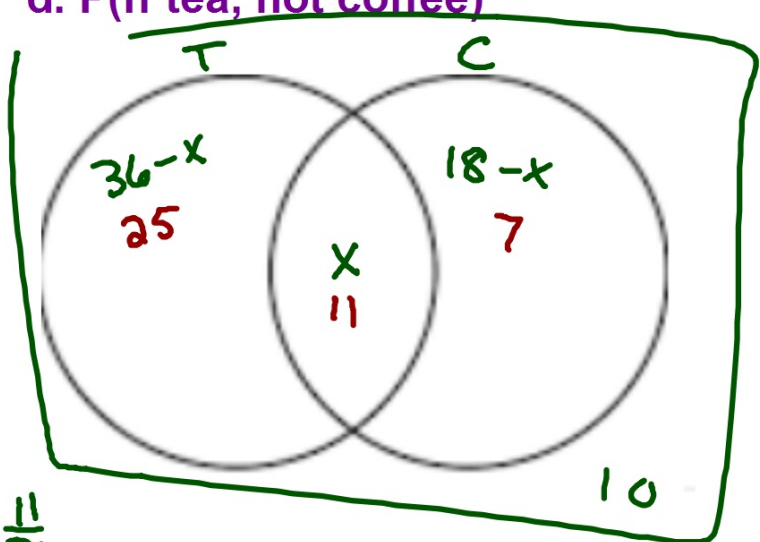
- How many drink both? 11
- P(Tea not coffee)
- P(If tea, coffee too)
- P(if tea, not coffee)

$$\begin{aligned}
 a) \quad & 36 - x + 18 - x + x + 10 = 53 \\
 & 64 - x = 53 \\
 & -x = -11 \\
 & x = 11
 \end{aligned}$$

$$b) \quad P(T \cap C') = \frac{25}{53}$$

$$\begin{aligned}
 c) \quad P(C | T) &= \frac{P(C \cap T)}{P(T)} \\
 &= \frac{\frac{11}{53}}{\frac{36}{53}} = \frac{11}{36}
 \end{aligned}$$

$$\begin{aligned}
 d) \quad P(C' | T) &= \frac{P(C' \cap T)}{P(T)} = \frac{\frac{25}{53}}{\frac{36}{53}} = \frac{25}{36}
 \end{aligned}$$



36 p. 87-88
#1,4,9