

$$5c \quad g(x) = x^2 + 3 \quad h(x) = x - 4$$

$$54) \quad (g \circ h)(x) = g(h(x)) \\ = g(x-4) = (x-4)^2 + 3$$

$$b) \quad (h \circ g)(x) = h(g(x)) = (x-4)(x-4) + 3 \\ h(x^2+3) = (x^2+3) - 4 = x^2 - 8x + 16 + 3 \\ = x^2 - 1 \quad = x^2 - 8x + 19$$

Solve

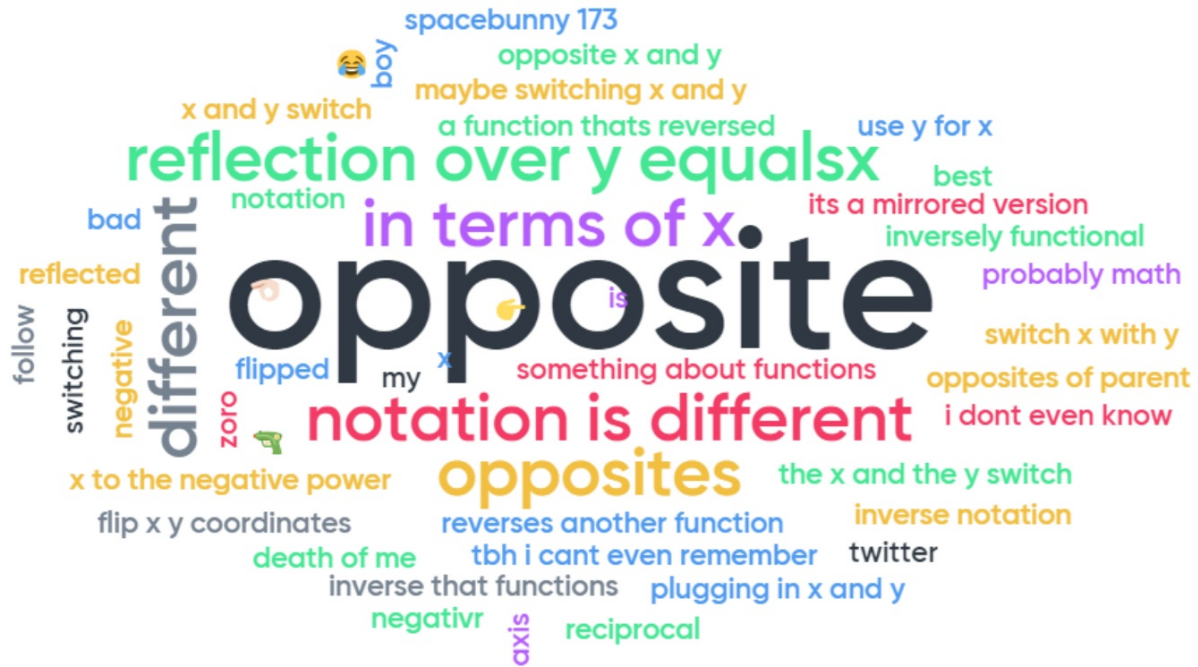
$$(g \circ h)(x) = (h \circ g)(x)$$

$$x^2 - 8x + 19 = x^2 - 1$$

$$-8x + 19 = -1$$

$$-8x = -20$$

$$x = \frac{20}{8} \text{ or } \frac{5}{2}$$



1.5 Inverse Functions

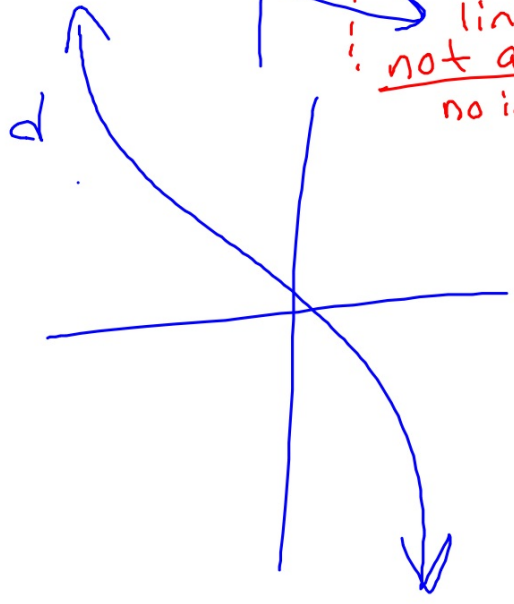
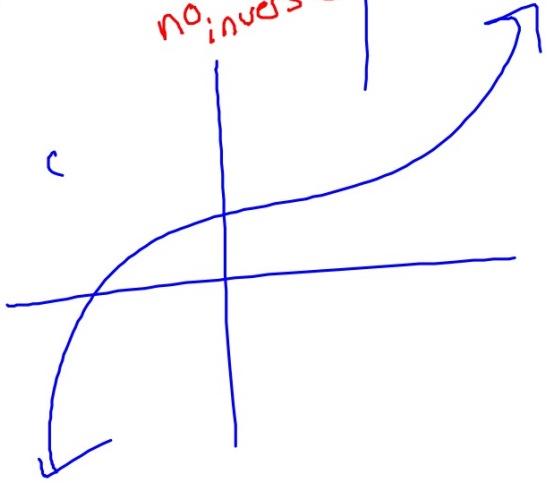
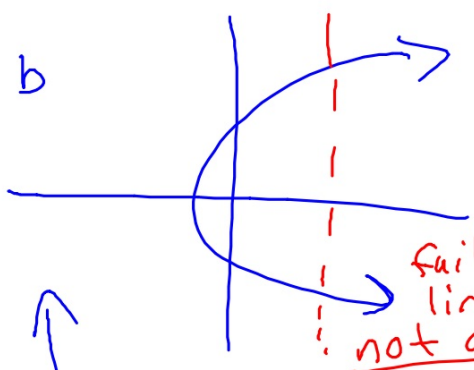
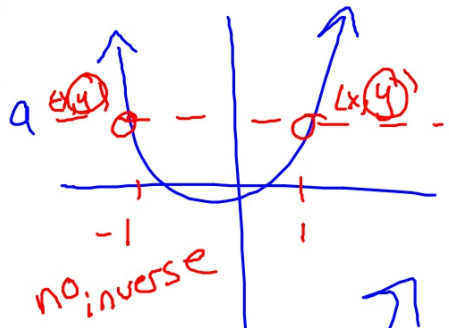
def The inverse of a function $f(x)$ is $f^{-1}(x)$. It reverses the action of $f(x)$

* In order to have an inverse, a relation must 1st be a function (1x maps to 1y) and
vertical line test

One-to-one (every y has 1x)
horizontal line test

Ex

Which have inverses?



fails vert. line
not a function
no inverse

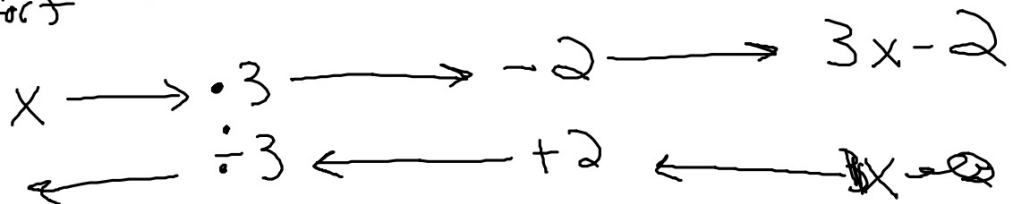
Function $f(x)$ and $g(x)$ are inverses of one another if:

$(f \circ g)(x) = x$ for all x in the domain
and $(g \circ f)(x) = x$ for all x in the domain

Finding Inverses Algebraically

action for f $f(x) = 3x - 2$

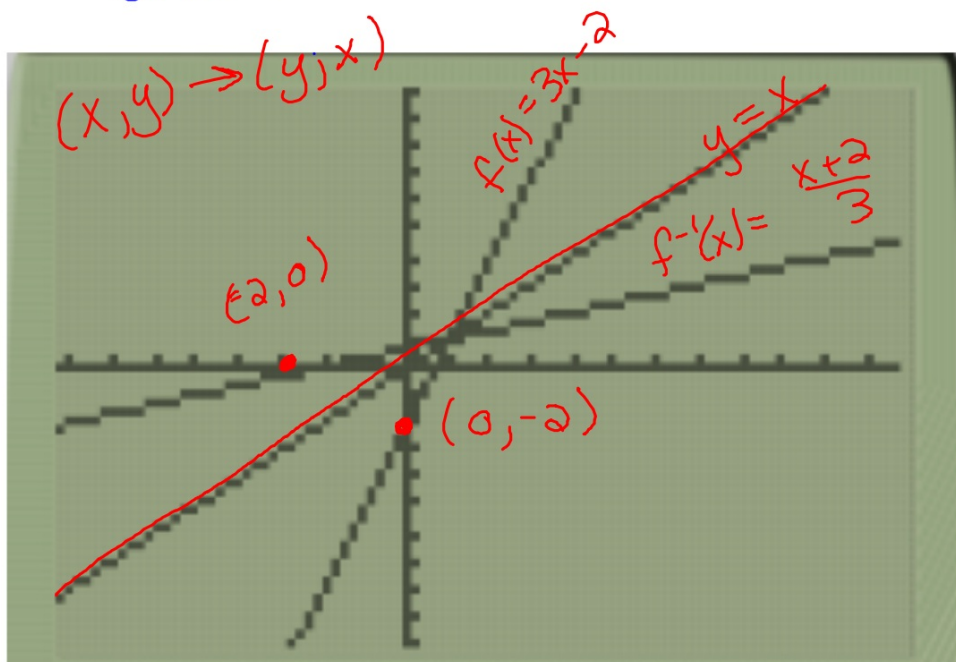
$$f^{-1}(x) = \frac{x+2}{3}$$



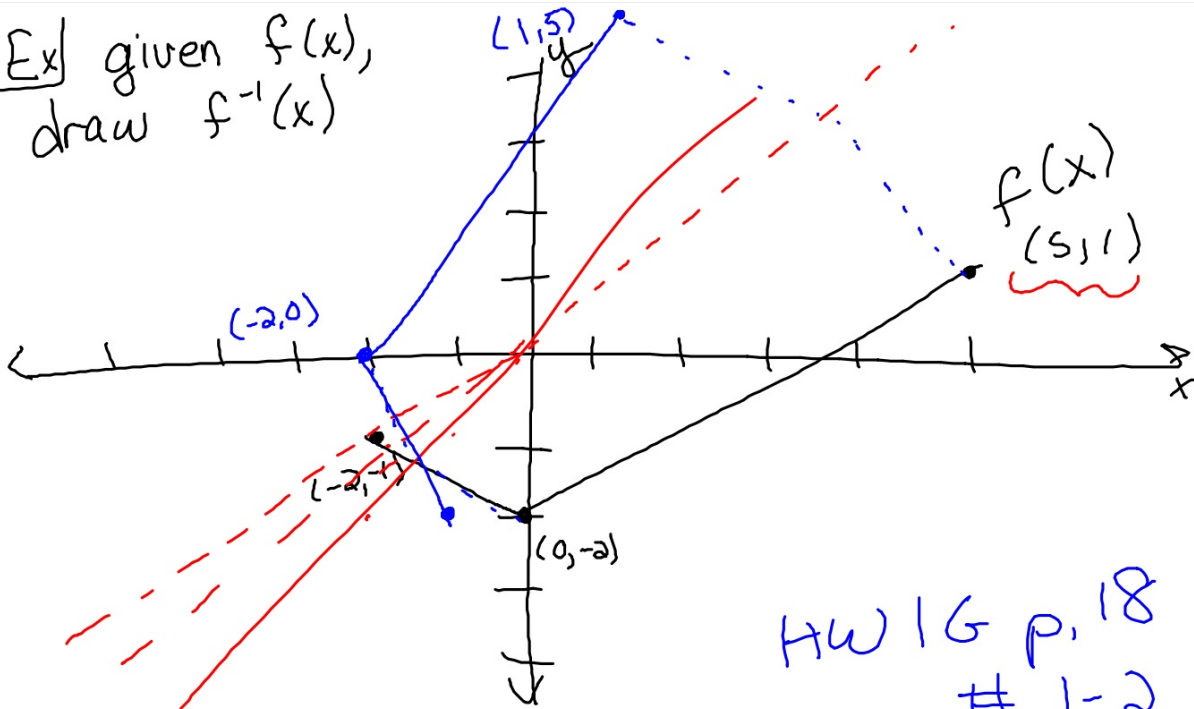
$$(f \circ f^{-1})(x) = \underline{\hspace{2cm}} \quad f(f^{-1}(x)) = 3\left(\frac{x+2}{3}\right) - 2$$

$$(f^{-1} \circ f)(x) = \frac{(3x-2)+2}{3} = \frac{3x}{3} = x \quad = x+2-2 = x$$

The graphs of $f(x)$ and $f^{-1}(x)$ will be reflected over the line $y = x$



Ex) given $f(x)$,
draw $f^{-1}(x)$



Pretend this
can have an
inverse

HW 16 p. 18
1-2